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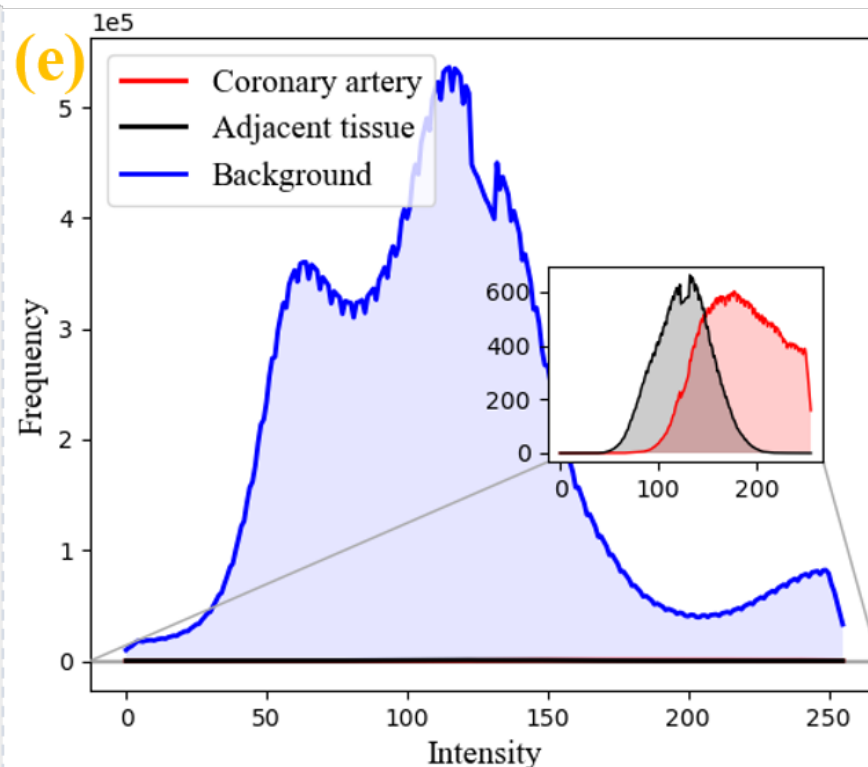
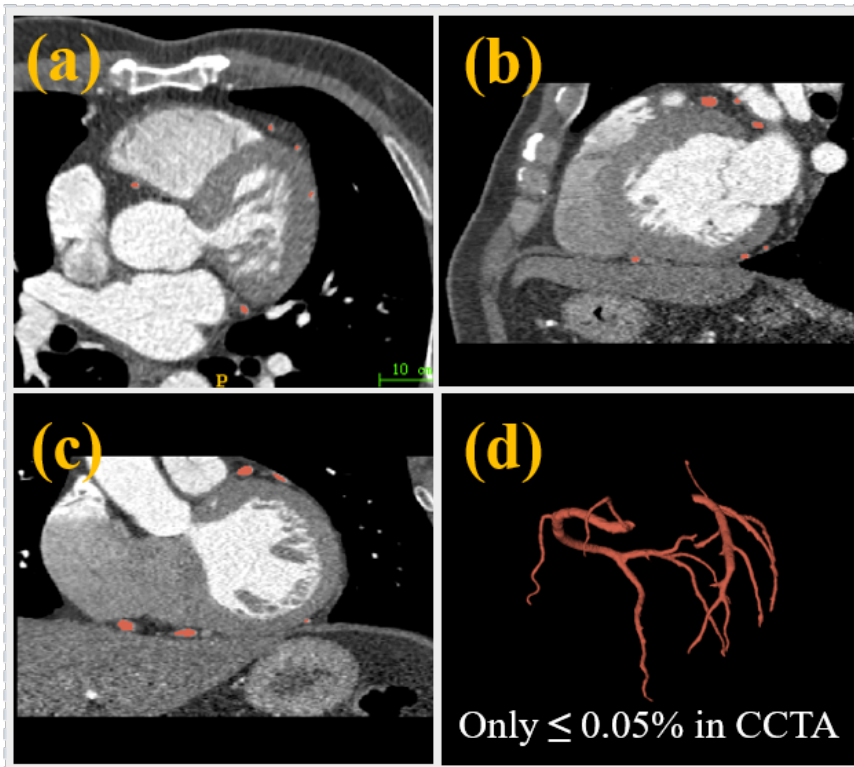


西安交通大学医学院  
XI'AN JIAOTONG UNIVERSITY COLLEGE OF MEDICINE

第二附属医院 (西北医院)

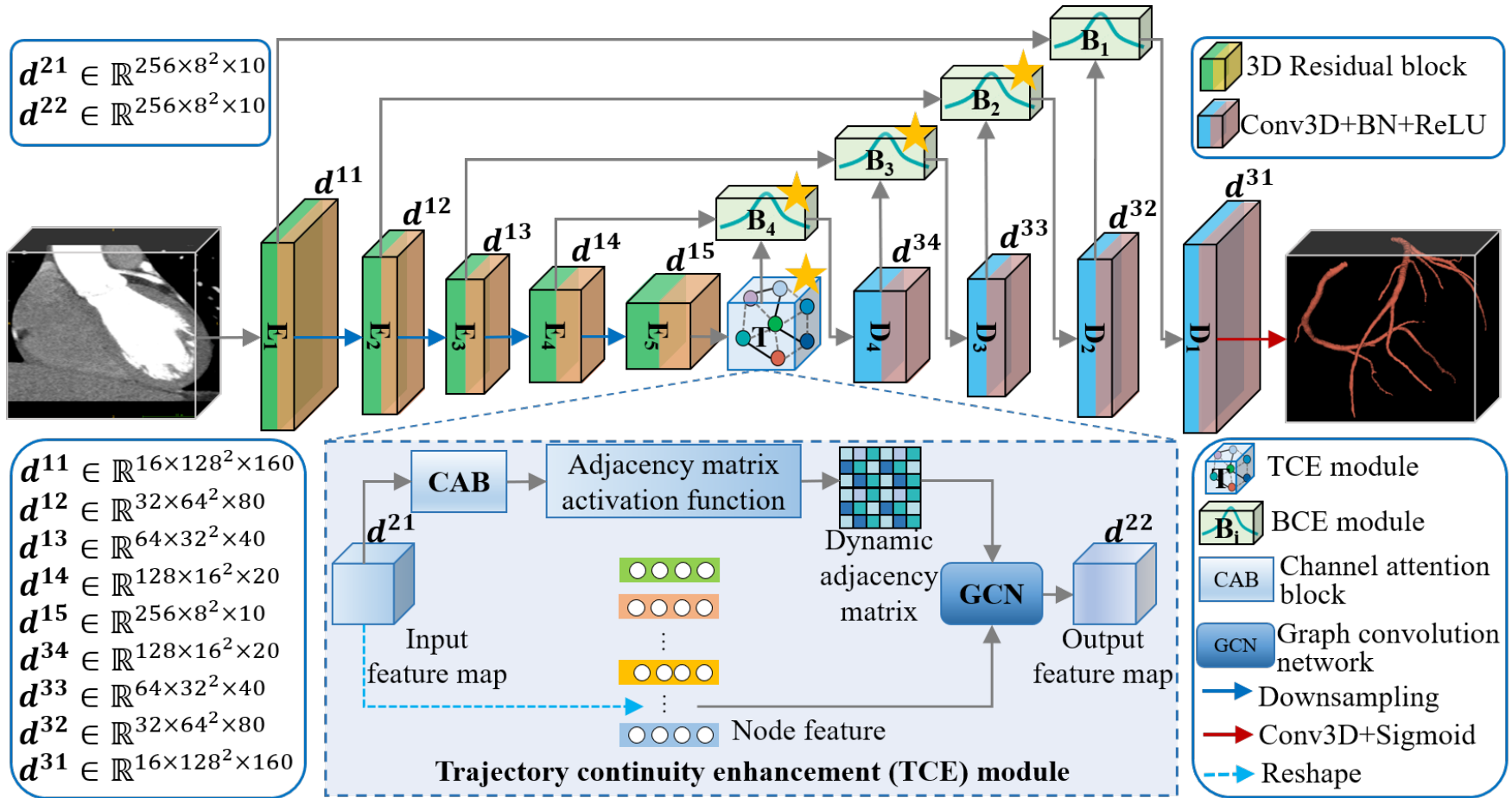
# High-quality coronary artery segmentation via fuzzy logic modeling coupled with dynamic graph convolutional network

汇报人：董彩霞  
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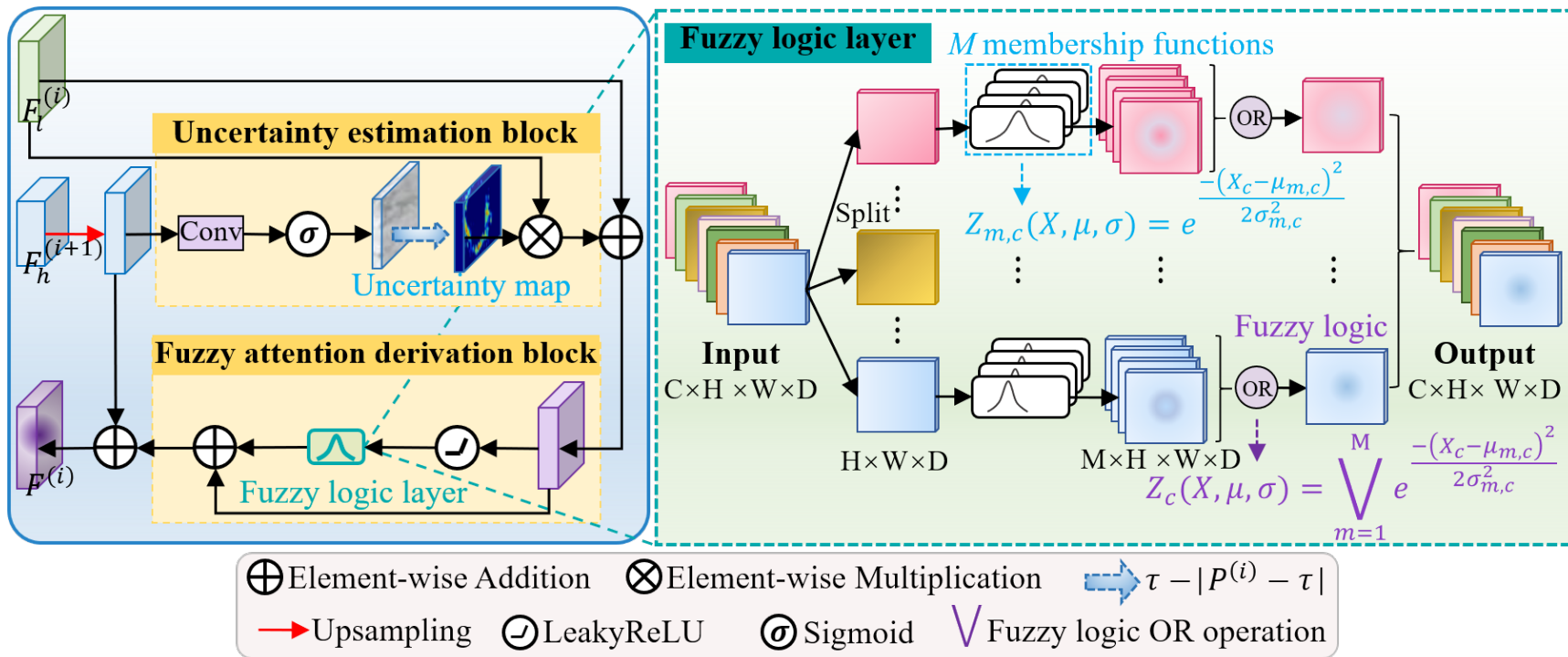
- Vessels are **thin structures** with lumen diameters ranging from 1 mm to 5 mm ((a)-(c)), leading to numerous **hard-to-segment regions and discontinuous segmentation**.
- The images have a **small volume ratio** (less than 0.05%, see (d)), which causes a severe imbalance between vessel and non-vessel pixels.
- The extremely **low contrast** in some vessel locations makes blood vessel boundaries ambiguous (1(e)).

# 方法: Framework



We propose a novel 3D deep network for high-quality CA segmentation that synergistically and comprehensively explores CA feature enhancement from the perspectives of **boundary completeness** and **trajectory continuity**, achieving a synergistic effect through the carefully orchestrated functioning of **fuzzy logic modeling** coupled with a **dynamic graph convolutional network**.

# 方法: Boundary Completeness Enhancement Module



We propose a BCE module that integrates fuzzy logic with the attention mechanism to help the segmentation network focus on the relevant region while **reducing uncertainty** and variations in feature representations to improve **boundary quality**. It consists of two blocks: the **uncertainty estimation block** and the **fuzzy attention derivation block**.

# 方法: Boundary Completeness Enhancement Module

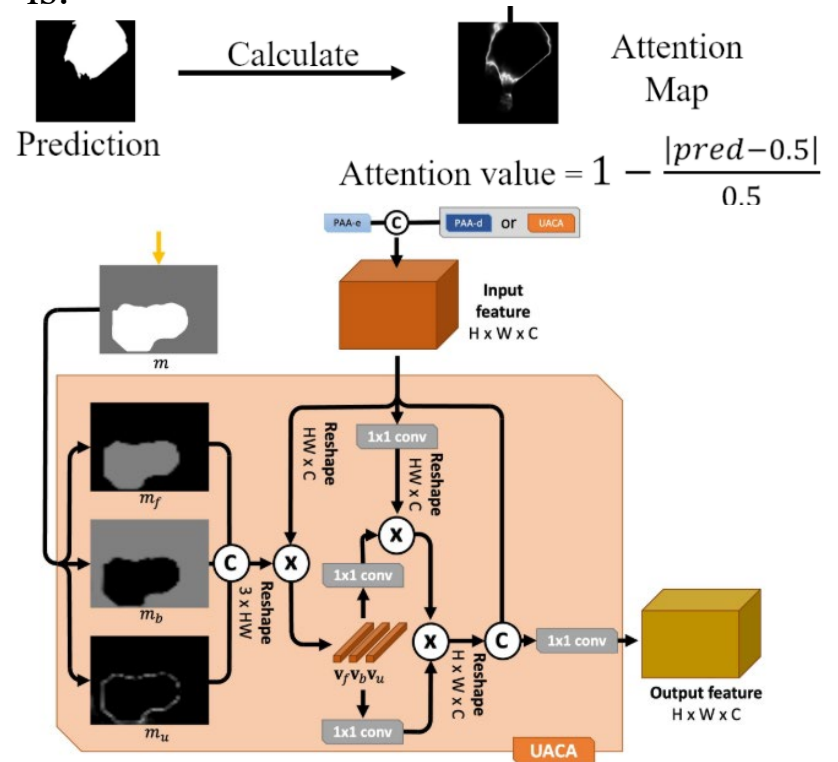
## Algorithm 1 Boundary Completeness Enhancement Module

**Input:** The low-level features  $F_l^{(i)}$  from encoder and high-level features  $F_h^{(i+1)}$  from decoder.

**Output:** The enhanced feature representation  $F^{(i)}$ .

- 1: Randomly initialize parameters  $\mu \in \mathbb{R}^{m \times C}$  and  $\delta \in \mathbb{R}^{m \times C}$  of membership functions  $Z(X, \mu, \sigma)$ .
- 2: Compute the probability map  $P^{(i)}$  from the upper layer  $F_h^{(i+1)}$  of the decoder stream based on Eq.2.
- 3: **for**  $j$  in  $H \times W \times D$  **do**
- 4:     Compute the uncertainty estimation map  $Unc_j^{(i)}$  based on Eq.1.
- 5:     **end for**     
$$F_{Unc}^{(i)} = (Unc^{(i)} \otimes F_l^{(i)}) \oplus F_l^{(i)}$$
- 6:     Compute the output  $F_{Unc}^{(i)}$  based on Eq.3.
- 7:     Compute the input  $X \in \mathbb{R}^{C \times H \times W \times D}$  of the fuzzy logic layer,  $X = \text{LeakyReLU}(F_{Unc}^{(i)})$ .
- 8:     **for**  $c$  in  $C$  **do**
- 9:         Compute the fuzzy membership degrees  $Z_c(X, \mu, \delta)$  based on Eq.4.
- 10:        Compute degrees  $Z_c(X, \mu, \delta)$  of  $c$ -th channel by adopting aggregation operator ‘OR’ to  $Z_c$  based on Eq.5.
- 11:     **end for**
- 12:     Compute the final result  $F^{(i)}$  of BCE based on Eq.6.

**Uncertainty map:** We believe that the closer the predicted value is to the threshold  $\tau$ , the more uncertain the prediction of the corresponding position is.



- Zhang R, et al. Adaptive context selection for polyp segmentation, MICCAI 2020.
- Kim T, Lee H, Kim D. Uacanet: Uncertainty augmented context attention for polyp segmentation, ACM International Conference on Multimedia. 2021: 2167-2175.

# 方法：Fundamentals of Fuzzy Logic

- **布尔逻辑的概念**：经典布尔逻辑指事物都可以用**二元项**（0或1，黑或白，是或否）来表达，而生活中，很多概念都无法用确定性的语言描述，**多与少，高于矮，年轻与年老**，这些都无法用具体的数值来进行衡量，具有模糊性。
- **模糊逻辑的概念**：模糊逻辑（Fuzzy Logic）是一种使用隶属度代替布尔真值的逻辑。模糊逻辑并不把一个命题直接分为真与假，而对于真与假的归属，可以用隶属度来进行衡量。**隶属度**是 $[0,1]$ 之间的一个取值，用来标识一个程度。
- **布尔与模糊逻辑运算对比**：

Boolean Logic	Fuzzy Logic
AND(x,y)	MIN(x,y)
OR(x,y)	MAX(x,y)
NOT(x)	1-x

- <https://blog.csdn.net/SweeNeil/article/details/86535572>
- <https://www.jianshu.com/p/b316acff0f02>

# 方法: Fuzzy attention derivation block

- For a specific channel  $c$ ,  $M$  **membership functions** are applied to each feature point in the channel. It should be noted that  $M$  is kept the same for each channel of the feature map and can vary between different input feature maps.

高斯隶属函数:  $Z_{m,c}(X, \mu, \delta) = e^{\frac{-(X_c - \mu_{m,c})^2}{2\delta_{m,c}^2}}$

- We employ the aggregation **operator 'OR'** to construct fuzzy feature representations, which can preserve the importance of target feature representations while eliminating irrelevant features.

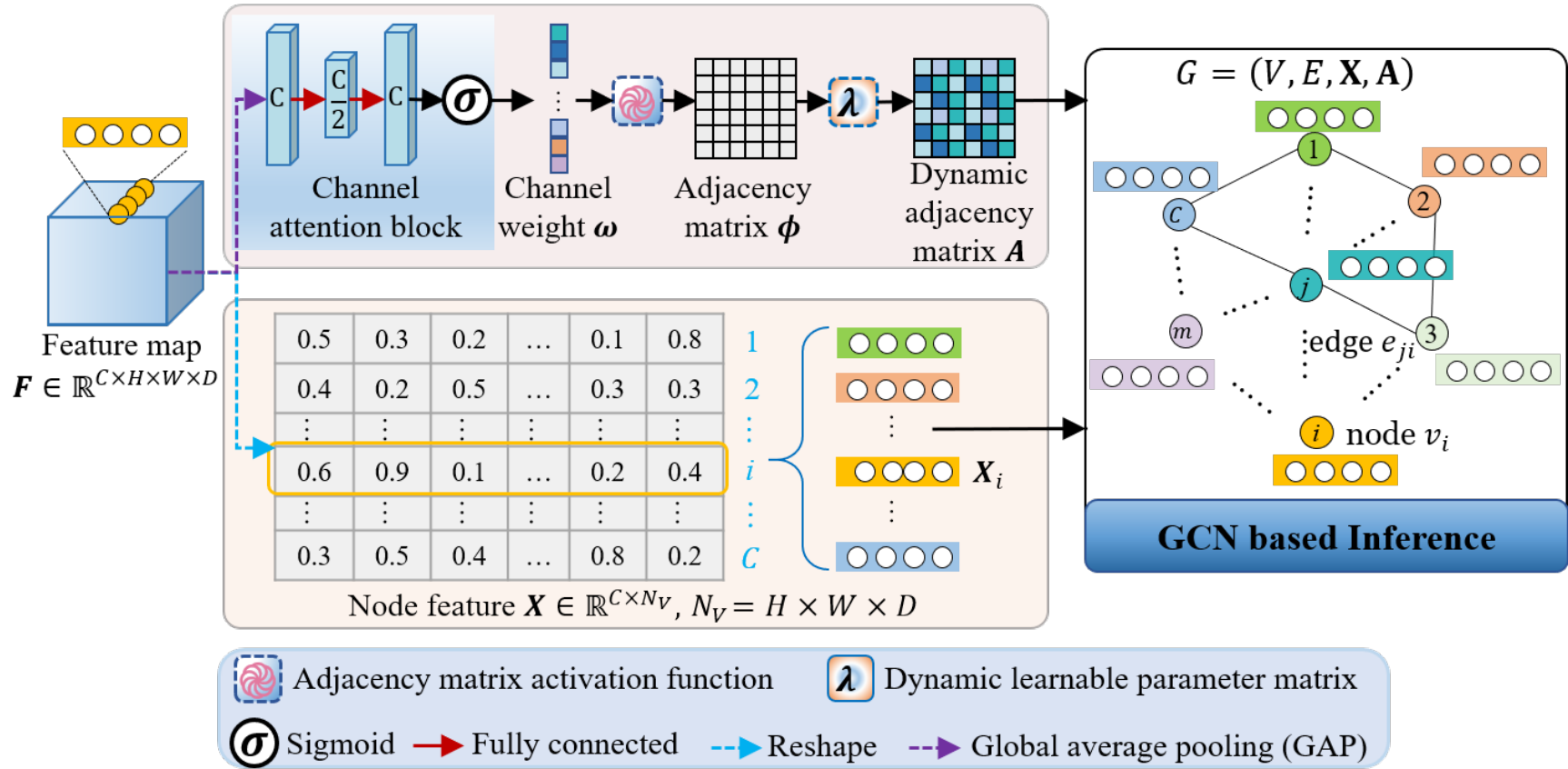
通过模糊逻辑或 ( OR ) 运算进行模糊特征表示:

$$Z_c(X, \mu, \delta) = \bigvee_{m=1}^M Z_{m,c}(X, \mu, \delta) = \bigvee_{m=1}^M e^{\frac{-(X_c - \mu_{m,c})^2}{2\delta_{m,c}^2}}$$
$$= \max \left( e^{\frac{-(x_c - \mu_{1,c})^2}{2\sigma_{1,c}^2}}, \dots, e^{\frac{-(X_c - \mu_{m,c})^2}{2\delta_{m,c}^2}}, \dots, e^{\frac{-(x_c - \mu_{M,c})^2}{2\delta_{M,c}^2}} \right)$$

- The fuzzy degree tensor:  $F_{Fuz}^{(i)} = \{Z_c(X, \mu, \delta)\}(c = 1, \dots, C)$
- The final result of the BCE module:

$$F^{(i)} = \left( F_{Unc}^{(i)} \oplus F_{Fuz}^{(i)} \right) \oplus UpSample \left( F_h^{(i+1)} \right)$$

# 方法: Trajectory Continuity Enhancement Module



We propose a TCE module embedded at the bottom of the network, built upon a 3D dynamic GCN with adaptive hyper-parameter optimization, capable of iteratively improving vessel trajectory continuity.

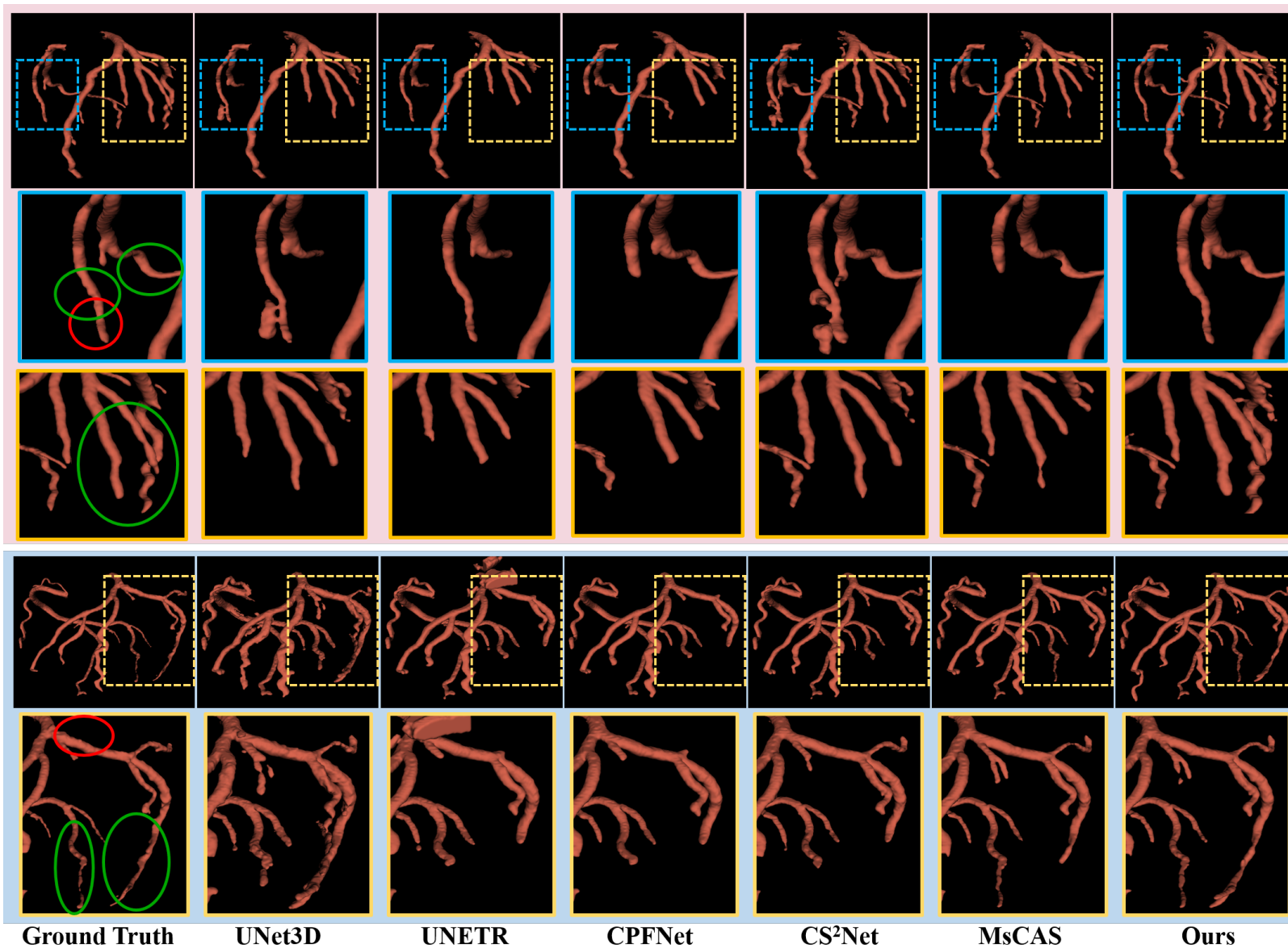


# 实验结果：定量结果

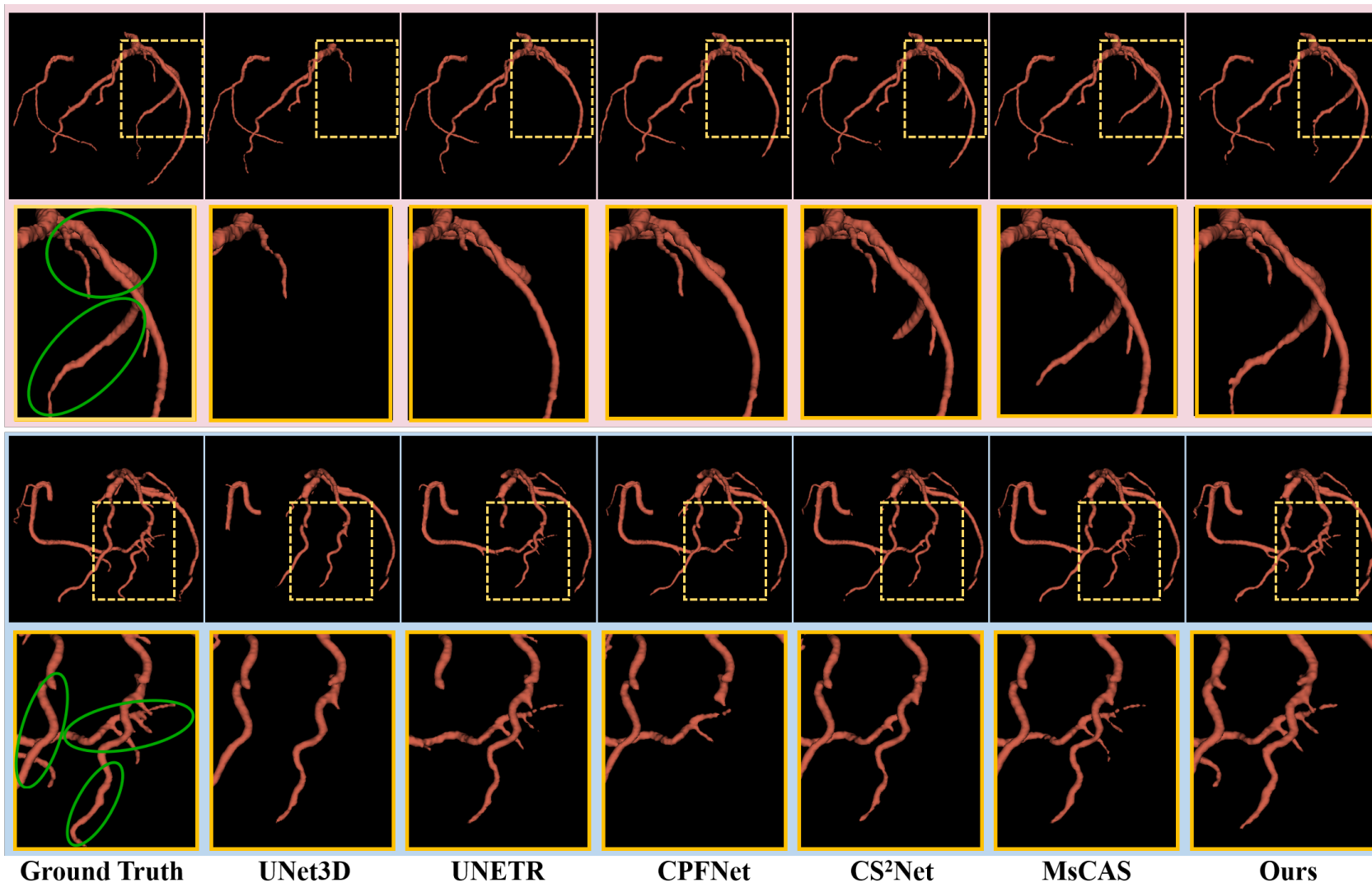
Table 1: The mean±std results of CA segmentation performance on the CAS-119 dataset and the ASOCA dataset by different methods. The best results are in **bold**, and the second-best results are underlined.

Datasets	Method	DSC (%)↑	TPR (%)↑	ASSD (mm)↓	TR (%)↑	TP (%)↑	p-value (DSC)
CAS-119	UNet3D (Çiçek et al., 2016)	81.65±0.73	88.16±0.78	1.56±0.05	87.93±0.98	90.04±0.82	$7.68 \times 10^{-5}$
	VNet (Milletari et al., 2016)	81.78±0.62	88.32±0.69	1.51±0.04	88.08±0.81	90.22±0.78	$8.35 \times 10^{-6}$
	HighResNet3D (Li et al., 2017)	82.57±0.84	88.49±0.73	1.31±0.06	88.15±0.58	90.95±0.66	$1.73 \times 10^{-5}$
	MedT (Valanarasu et al., 2021)	82.22±0.77	88.72±0.63	1.58±0.07	89.74±0.61	90.62±0.74	$7.66 \times 10^{-4}$
	TransBTS (Wang et al., 2021)	82.53±0.72	88.79±0.55	1.52±0.05	89.12±0.72	90.94±0.83	$8.92 \times 10^{-4}$
	Unetr (Hatamizadeh et al., 2022)	83.01±0.57	89.14±0.53	1.41±0.06	89.77±0.85	91.07±0.79	$1.36 \times 10^{-5}$
	CA-Net (Gu et al., 2020)	83.67±0.84	89.87±0.55	1.42±0.06	89.93±0.69	91.84±0.88	$7.69 \times 10^{-4}$
	MTLN (Zhang et al., 2021)	83.72±0.78	89.93±0.81	1.19±0.05	89.76±0.78	91.93±0.94	$9.55 \times 10^{-5}$
	CPFNet (Feng et al., 2020)	84.01±0.68	90.31±0.45	1.08±0.06	<u>90.36±0.82</u>	92.87±0.86	$1.37 \times 10^{-4}$
	DenseVoxelNet (Yu et al., 2017)	83.35±0.58	88.72±0.67	1.13±0.05	89.85±1.02	91.64±0.85	$7.43 \times 10^{-4}$
	CS <sup>2</sup> Net (Mou et al., 2021)	84.34±0.46	<u>90.76±0.84</u>	1.02±0.05	90.25±0.83	<u>92.95±0.89</u>	$1.85 \times 10^{-4}$
MsCAS (Dong et al., 2022)	<u>84.58±0.45</u>	89.39±0.34	<u>0.83±0.04</u>	90.05±0.74	92.74±0.92	$8.92 \times 10^{-4}$	
BT-Net	<b>86.27±0.31</b>	<b>92.31±0.27</b>	<b>0.79±0.04</b>	<b>92.37±0.59</b>	<b>95.16±0.75</b>	–	
ASOCA	UNet3D (Çiçek et al., 2016)	83.84±0.81	88.51±0.83	1.21±0.12	87.84±0.85	90.36±0.77	$6.47 \times 10^{-6}$
	VNet (Milletari et al., 2016)	83.96±0.94	88.73±0.65	1.26±0.10	88.36±0.76	90.57±0.72	$2.13 \times 10^{-5}$
	HighResNet3D (Li et al., 2017)	84.25±0.87	89.26±0.68	1.19±0.08	88.72±0.49	91.25±0.67	$6.52 \times 10^{-4}$
	MedT (Valanarasu et al., 2021)	84.43±0.82	89.34±0.81	1.27±0.10	88.65±0.65	90.91±0.59	$7.82 \times 10^{-5}$
	TransBTS (Wang et al., 2021)	84.76±1.04	89.68±0.84	1.23±0.11	89.06±0.73	91.21±0.67	$8.77 \times 10^{-5}$
	Unetr (Hatamizadeh et al., 2022)	85.22±0.91	88.11±0.77	1.16±0.07	89.49±0.56	92.35±0.54	$1.65 \times 10^{-4}$
	CA-Net (Gu et al., 2020)	85.85±0.86	90.64±0.63	1.61±0.08	90.89±0.82	92.78±0.79	$9.52 \times 10^{-4}$
	MTLN (Zhang et al., 2021)	85.91±0.79	91.05±0.67	1.05±0.11	90.82±0.92	92.89±1.01	$5.37 \times 10^{-4}$
	CPFNet (Feng et al., 2020)	86.23±0.72	<u>91.24±0.52</u>	0.86±0.09	<u>91.37±0.76</u>	93.52±0.78	$4.57 \times 10^{-4}$
	DenseVoxelNet (Yu et al., 2017)	85.54±0.88	90.21±0.69	0.85±0.10	90.91±0.96	92.72±1.16	$9.36 \times 10^{-5}$
	CS <sup>2</sup> Net (Mou et al., 2021)	<u>86.67±0.91</u>	91.01±0.72	0.81±0.07	91.32±0.79	<u>93.56±0.78</u>	$3.28 \times 10^{-4}$
MsCAS (Dong et al., 2022)	86.53±0.68	90.85±0.46	<u>0.78±0.09</u>	91.11±0.68	93.44±0.86	$5.81 \times 10^{-4}$	
BT-Net	<b>88.78±0.44</b>	<b>92.86±0.43</b>	<b>0.57±0.08</b>	<b>92.46±0.63</b>	<b>94.67±0.56</b>	–	

# 实验结果：定性结果CAS-119 数据集



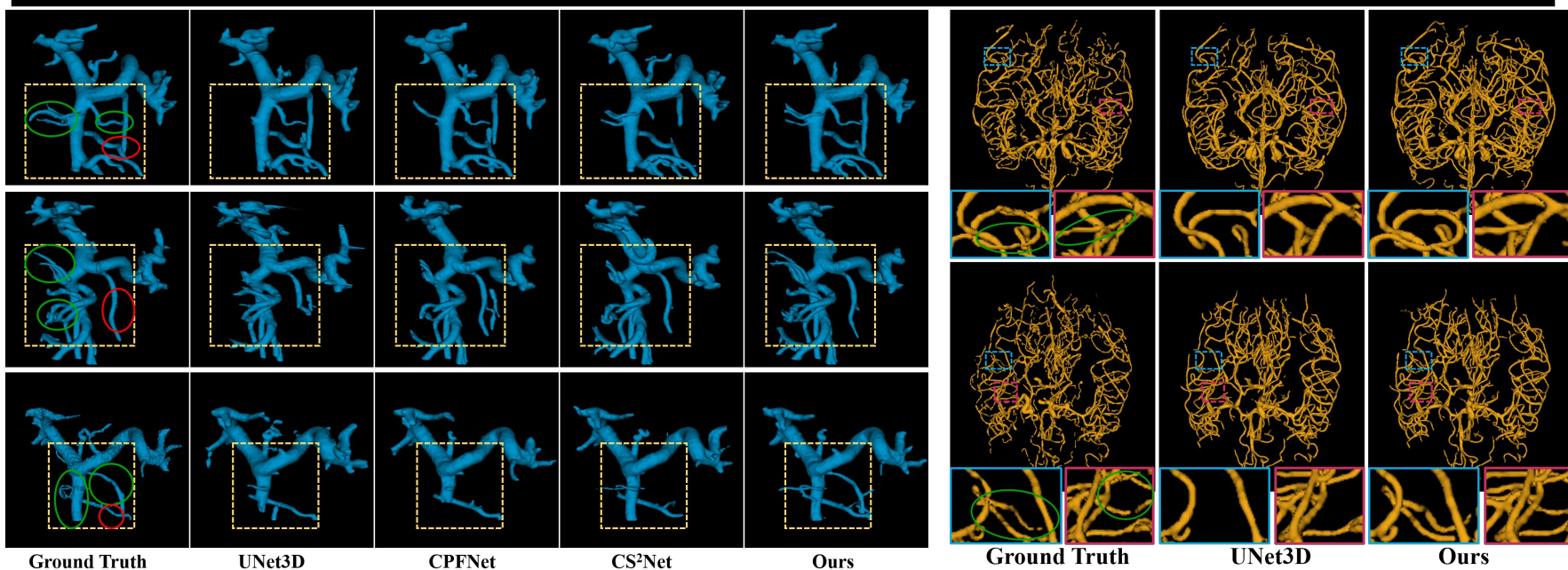
# 实验结果：定性结果ASOCA 数据集



# 实验结果：其他血管数据集

Table 2: Quantitative comparison of our method with other methods on the PVS-203 and MIDAS datasets. The best results are in bold.

Datasets	Method	DSC (%) $\uparrow$	TPR (%) $\uparrow$	ASSD (mm) $\downarrow$	TR (%) $\uparrow$	TP (%) $\uparrow$	p-value (DSC)
PVS-203	UNet3D (Çiçek et al., 2016)	87.02 $\pm$ 0.46	85.76 $\pm$ 0.56	1.42 $\pm$ 0.11	87.09 $\pm$ 0.53	87.94 $\pm$ 0.67	$6.48 \times 10^{-5}$
	VNet (Milletari et al., 2016)	87.51 $\pm$ 0.47	86.22 $\pm$ 0.52	1.38 $\pm$ 0.09	87.60 $\pm$ 0.55	88.12 $\pm$ 0.64	$5.59 \times 10^{-5}$
	CPFNet (Feng et al., 2020)	89.24 $\pm$ 0.42	88.57 $\pm$ 0.49	1.29 $\pm$ 0.10	91.34 $\pm$ 0.61	90.85 $\pm$ 0.62	$3.27 \times 10^{-4}$
	CS <sup>2</sup> Net (Mou et al., 2021)	90.01 $\pm$ 0.38	90.15 $\pm$ 0.47	1.21 $\pm$ 0.09	91.27 $\pm$ 0.55	91.88 $\pm$ 0.56	$8.76 \times 10^{-3}$
	<b>BT-Net</b>	<b>91.44<math>\pm</math>0.35</b>	<b>92.78<math>\pm</math>0.44</b>	<b>1.16<math>\pm</math>0.08</b>	<b>93.12<math>\pm</math>0.52</b>	<b>94.61<math>\pm</math>0.57</b>	–
MIDAS	UNet3D (Çiçek et al., 2016)	66.72 $\pm$ 0.73	73.38 $\pm$ 0.64	1.53 $\pm$ 0.10	78.44 $\pm$ 0.83	81.64 $\pm$ 0.82	$1.54 \times 10^{-3}$
	VNet (Milletari et al., 2016)	67.01 $\pm$ 0.68	73.22 $\pm$ 0.67	1.49 $\pm$ 0.12	78.57 $\pm$ 0.76	81.86 $\pm$ 0.76	$8.81 \times 10^{-4}$
	CPFNet (Feng et al., 2020)	68.56 $\pm$ 0.71	74.61 $\pm$ 0.59	1.30 $\pm$ 0.09	80.12 $\pm$ 0.78	83.13 $\pm$ 0.79	$5.32 \times 10^{-3}$
	CS <sup>2</sup> Net (Mou et al., 2021)	69.33 $\pm$ 0.69	75.41 $\pm$ 0.52	1.22 $\pm$ 0.12	80.60 $\pm$ 0.75	83.77 $\pm$ 0.81	0.027
	<b>BT-Net</b>	<b>71.82<math>\pm</math>0.65</b>	<b>76.39<math>\pm</math>0.48</b>	<b>1.14<math>\pm</math>0.10</b>	<b>82.12<math>\pm</math>0.64</b>	<b>85.92<math>\pm</math>0.78</b>	–





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谢谢！

