#### A Tutorial on Transfer Learning

Yang Li 2019/11/26

# Today's Talk

- What's Transfer Learning
- Transfer Learning Techniques
  - Task transfer learning
  - Domain adaptation
  - Transfer bound on domain adaptation
- How to avoid negative transfer?
  - Case study on feature transferability
  - Task transferability: empirical and theoretical methods
- Discussions and Q&A







# Machine Learning

Image gradier Example. Image-based recognition task

#### Traditional machine learning flow





End-to-end learning with deep neural netes

### Single-Task Machine Learning

ImageNet competition results over the years



# Single-Task Machine Learning



image credit: https://arxiv.org/abs/1605.07678

#### Issues with Single-Task Learning

- Learn something new quickly: can't train from scratch every time
- Most classes/tasks have very few data samples
- Training labels may be expensive to obtain





# Transfer learning

Human learners can inherently transfer knowledge between tasks



How can machines recognize and apply relavent knowledge from previous learning experience?

### Transfer Learning at 1000 feet

• Transfer knowledge from one or more source domains/tasks to a target domain/task.



# How transfer might improve target learnring



Transfering might reduce target learning performance (negative transfer)

# Two Branches of Transfer Learning Paradigms

**Inductive Learning:** Learn decision function f from training data, test on unseen data

$$x \longrightarrow f \longrightarrow y$$

Reinforcement Learning: sequential decision making problems



# Inductive Transfer Learning Examples

- Domain-specific computer vision tasks
- Common to transfer pre-trained features from ImageNet



(a) No damage



# ImageNet 1000-class classification task







(b) Flexural dama; ;e



(c) Shear damage



(d) Combined damage Structural Damage Detection

Yuqing Zhao et. al. Deep Transfer Learning for Image-Based Structural Damage Recognition





#### **K-Shot Learning**



# Reinforcement Transfer Learning Examples

- Reinforcement learning for robotic control, e.g
  - SIMtoReal : transfer knowledge from simulated robot to physical robot





Simulated marble maze game

Real maze on robotic arm

# **Applications of Transfer Learning**

- Reinforcement learning for robotic control, e.g
  - Transfer between robots and between tasks



Devin (2016) Learning Modular Neural Network Policies for Multi-Task Multi-Robot Transfer

# Transfer Learning vs Multi-Task Learning

TL is more likely to encounter in real world than MTL



Sequential learning: focus on target task Joint learning: focus on all tasks

# Today's Talk

- What's Transfer Learning
- Transfer Learning Techniques
  - Task transfer learning
  - Domain adaptation
  - Transfer bound on domain adaptation
- How to avoid negative transfer?
  - Case study on feature transferability
  - Task transferability: empirical and theoretical methods
- Discussions and Q&A

# **Transfer Learning Definition**



Transfer learning: improve the performance of predictive function  $f_t$  for  $T_t$  by discover and transfer latent knowledge from  $(D_s, T_s)$ , where  $D_s \neq D_t$  and/or  $T_s \neq T_t$ 

#### **Transfer Learning**



Task Transfer Learning: adapt source hypothesis or feature to target task



#### **Transfer Learning**



**Domain adaptation:** Learn domain agnostic representations

#### T<sub>s</sub>/T<sub>t</sub>: Vehicle Detection



D<sub>t</sub> (night)

#### **Transfer Learning**



Task Transfer Learning: adapt source hypothesis or feature to target task

**Domain adaptation:** Learn domain agnostic representations

Most transfer learning problems in practice are hybrid!

# Task Transfer Learning

Pretrained Model + Fine Tuning

e.g object classification -> scene classification



intuition: low level features are shared across most vision tasks

# Heterogeneous Task Transfer Learning

 Heterogeneous task transfer learning using encoder-decoder network



# Today's Talk

- What's Transfer Learning
- Transfer Learning Techniques
  - Task transfer learning
  - Domain adaptation
  - Transfer bound on domain adaptation
- How to avoid negative transfer?
  - Case study on feature transferability
  - Task transferability: empirical and theoretical methods
- Discussions and Q&A

# **Domain Adaptation Techniques**

Instance-based approach

- Mapping-based approach
- Target Domain

arget Domain





Adversarial-based approach

#### Instance-based approaches

 select partial instances from the source domain as supplements to the training set in the target domain



Partial instances in the source domain can be utilized by the target domain with appropriate weights

# Boosting for instance-based transfer

- TrAdaBoost (Dai 2007)
  - Use AdaBoost to filter out source domain instances that are dissimilar to target domain
  - Reweight source domain instances to resemble target domain distribution
  - Train model with reweighted source + target domain instances



• TaskTrAdaBoost (2010): a boosting technique for transferring from multiple sources

# Mapping-based approach

 Mapping instances from the source domain and target domain into a new data space



# Maximal Mean Discrepency (MMD)

 Maximal Mean Discrepency : a kernel-based 2 sample test for the null hypothesis P=Q (Fortet and Mourier, 1953)

$$D_{MMD}[P,Q] \triangleq \sup_{\phi \in \mathcal{F}} \left( \mathbb{E}_{P}[\phi(X)] - \mathbb{E}_{Q}[\phi(Y)] \right)$$

- where  $X \sim P, Y \sim Q$
- feature map  $\phi(\cdot)$
- Used in Transfer Component Analysis (TCA) (Yang, 2018) to correct domain shift

$$D_{MMD}(X_S, X_T) = \left\| \frac{1}{N_S} \sum_{x_s \in X_S} \phi(x_s) - \frac{1}{N_T} \sum_{x_t \in X_T} \phi(x_t) \right\|_{\mathcal{H}}$$

### Use MMD as a Domain Regularization Term

• Given pre-trained source model, train an adpation network that minimizes classification error and domain MMD

$$L = L_C(X_L, y) + \lambda D_{MMD}^2(X_S, X_T)$$



Tzeng et. al. Deep Domain Confusion: Maximizing for Domain Invariance

# Use MMD as a Domain Regularization Term

- Training step:
  - 1. Select the layer to transfer from using MMD metric
  - 2. Train an adaptation layer f<sub>a</sub> on source and target data using MMD as a regularizer
- Testing step:
  - Transform target input by  $f_a(X_T)$



$$L = L_C(X_L, y) + \lambda D_{MMD}^2(X_S, X_T)$$

Tzeng et. al. Deep Domain Confusion: Maximizing for Domain Invariance

# Variations with MMD-based domain adaptation

- Deep Adaptation Network (Long et.al. 2015):
  - Use multi-kernel MMD (MK-MMD)  $D_{MMD}[P, Q, K] \triangleq \|(\mathbb{E}_{P}[\phi(X)] - \mathbb{E}_{Q}[\phi(Y)])\|_{\mathcal{H}_{K}}$
  - Fine-tune source task jointly with MMD constraints on multiple layers



- Joint Adaptation (2018): adapt joint distributions instead of  $P(X_{s}),\,Q(X_{t})$ 

# Comparisons of MMD-based domain adaptation methods

Office+Caltech Benchmark

Amazon	DSLR	Webcam	Caltech-256
6-6-	1		

Tuble 1. Clubbilleuton ucculue ( ()) on office of culuber for unsuper fised domain ucuptution (Them et and Resi et	Table 1.	Classification accuracy	(%) on Office-31	dataset for unsupervised	domain adaptation	(AlexNet and ResNet)
--	----------	-------------------------	------------------	--------------------------	-------------------	----------------------

Method	$\mathbf{A} \to \mathbf{W}$	$\mathrm{D} \to \mathrm{W}$	$W \to D$	$A \rightarrow D$	$D \rightarrow A$	$W \rightarrow A$	Avg
AlexNet (Krizhevsky et al., 2012)	$61.6 \pm 0.5$	95.4±0.3	99.0±0.2	$63.8 \pm 0.5$	51.1±0.6	$49.8 \pm 0.4$	70.1
TCA (Pan et al., 2011)	$61.0 {\pm} 0.0$	$93.2{\pm}0.0$	$95.2{\pm}0.0$	$60.8 {\pm} 0.0$	$51.6 \pm 0.0$	$50.9 {\pm} 0.0$	68.8
GFK (Gong et al., 2012)	$60.4 {\pm} 0.0$	$95.6 {\pm} 0.0$	$95.0{\pm}0.0$	$60.6 {\pm} 0.0$	$52.4 \pm 0.0$	$48.1 \pm 0.0$	68.7
DDC (Tzeng et al., 2014)	$61.8 {\pm} 0.4$	$95.0 {\pm} 0.5$	$98.5 {\pm} 0.4$	$64.4 \pm 0.3$	$52.1 \pm 0.6$	$52.2 \pm 0.4$	70.6
DAN (Long et al., 2015)	$68.5 {\pm} 0.5$	$96.0 \pm 0.3$	99.0±0.3	$67.0 \pm 0.4$	$54.0 \pm 0.5$	$53.1 \pm 0.5$	72.9
RTN (Long et al., 2016)	$73.3 \pm 0.3$	<b>96.8</b> ±0.2	<b>99.6</b> ±0.1	$71.0 \pm 0.2$	$50.5 \pm 0.3$	$51.0 \pm 0.1$	73.7
RevGrad (Ganin & Lempitsky, 2015)	$73.0 {\pm} 0.5$	$96.4{\pm}0.3$	$99.2 \pm 0.3$	$72.3 \pm 0.3$	$53.4 \pm 0.4$	$51.2 \pm 0.5$	74.3
JAN (ours)	$74.9 \pm 0.3$	$96.6 {\pm} 0.2$	$99.5 {\pm} 0.2$	$71.8 {\pm} 0.2$	<b>58.3</b> ±0.3	$55.0 \pm 0.4$	76.0
JAN-A (ours)	<b>75.2</b> ±0.4	96.6±0.2	<b>99.6</b> ±0.1	<b>72.8</b> ±0.3	$57.5 \pm 0.2$	<b>56.3</b> ±0.2	76.3
ResNet (He et al., 2016)	$68.4{\pm}0.2$	96.7±0.1	99.3±0.1	$68.9 \pm 0.2$	$62.5 \pm 0.3$	$60.7 \pm 0.3$	76.1
TCA (Pan et al., 2011)	$72.7 \pm 0.0$	$96.7 {\pm} 0.0$	$99.6 {\pm} 0.0$	$74.1 \pm 0.0$	$61.7 \pm 0.0$	$60.9 {\pm} 0.0$	77.6
GFK (Gong et al., 2012)	$72.8 {\pm} 0.0$	$95.0 {\pm} 0.0$	$98.2{\pm}0.0$	$74.5 {\pm} 0.0$	$63.4 {\pm} 0.0$	$61.0 {\pm} 0.0$	77.5
DDC (Tzeng et al., 2014)	$75.6 {\pm} 0.2$	$96.0 {\pm} 0.2$	$98.2{\pm}0.1$	$76.5 \pm 0.3$	$62.2 \pm 0.4$	$61.5 \pm 0.5$	78.3
DAN (Long et al., 2015)	$80.5 {\pm} 0.4$	97.1±0.2	99.6±0.1	$78.6 {\pm} 0.2$	$63.6 {\pm} 0.3$	$62.8 {\pm} 0.2$	80.4
RTN (Long et al., 2016)	$84.5 \pm 0.2$	$96.8 {\pm} 0.1$	99.4±0.1	$77.5 \pm 0.3$	$66.2 \pm 0.2$	$64.8 \pm 0.3$	81.6
RevGrad (Ganin & Lempitsky, 2015)	$82.0 {\pm} 0.4$	$96.9 {\pm} 0.2$	99.1±0.1	$79.7 \pm 0.4$	$68.2 {\pm} 0.4$	$67.4 {\pm} 0.5$	82.2
JAN (ours)	$85.4{\pm}0.3$	<b>97.4</b> ±0.2	<b>99.8</b> ±0.2	$84.7 \pm 0.3$	$68.6 {\pm} 0.3$	$70.0 {\pm} 0.4$	84.3
JAN-A (ours)	<b>86.0</b> ±0.4	96.7±0.3	99.7±0.1	<b>85.1</b> ±0.4	<b>69.2</b> ±0.4	<b>70.7</b> ±0.5	84.6

Long et. al. (2017). Deep Transfer Learning with Joint Adaptation Networks.

# Adversarial-based approach

• Adopt adversarial training in learning transferable representation.



Effective features should be discriminative for the main learning task and indiscriminative between the source domain and target domain.

# Adversarial-based approach

Ajakan et al. (2014) Domain-adversarial neural networks.

• Standard deep neural network training



# Domain Adversarial Neural Networks

Ajakan et al. (2014) Domain-adversarial neural networks.

• Gradient Reversal



#### Domain Adversarial Neural Networks (DANN) Ajakan et al. (2014) Domain-adversarial neural networks.

• DNN adapted feature distribution

source domain (MINIST)

target domain (MNIST-M)



**TSNE** visualization of CNN extracted features





# **Domain Adaptation Discussion**

- Instance-based approach: select and reweight instances in the source domain to be similar to the target distribution
   easy to implement, work with any base classifiers
- Mapping-based approach: map source and target data to latent space where source and target domains are similar easy to incorporate to neural network training
- Adversarial-based approach: find features that are indiscriminative between source and target domains good performance in computer vision

Why does such methods work?

A detour to learning theory



#### Transfer Bounds for Domain Adaptation

- Given input  $x \sim D$  with discrete alphabet  $\mathcal{X}$  and label  $y \in \{0,1\}$
- A hypothesis is a function  $h : \mathcal{X} \to \{0,1\}$
- Error (risk) of hypothesis *h* :

$$\epsilon(h) = \mathbb{E}_{x \sim D}[|h(x) - y|]$$

Empirical risk of hypothesis h given N samples (x<sub>i</sub>, y<sub>i</sub>) drawn
 i.i.d. from D:

$$\hat{\epsilon}(h) = \frac{1}{N} \sum_{i=1}^{N} |h(x_i) - y_i|$$

- Source risk:  $\epsilon_S(h) = \mathbb{E}_{x_S \sim P}[|h(x_S) y_S|]$
- Target risk:  $\epsilon_T(h) = \mathbb{E}_{x_T \sim Q}[|h(x_T) y_T|]$

# Transfer Bounds for Domain Adaptation

Ben-David et.al. (2010). A theory of learning from different domains

**Theorem.** Let  $h \in \mathcal{H}$  be a hypothesis,  $\epsilon_S(h)$  and  $\epsilon_T(h)$  be risks of source and target respectively, then

$$\epsilon_T(h) \le \epsilon_S(h) + d_{\mathcal{H}}(P,Q) + C_0 \quad \leftarrow \begin{array}{c} C_0: \text{ a constant for the} \\ \text{complexity of } \mathcal{H} \end{array}$$

where

$$d_{\mathcal{H}}(P,Q) \triangleq 2 \sup_{\eta \in \mathcal{H}} \left| \Pr_{P}[\eta(x_{S}) = 1] - \Pr_{Q}[\eta(x_{T}) = 1] \right|$$

is the H-divergence between P and Q.

Lemma. The H-divergence can be bounded by the empirical estimate:

$$d_{\mathcal{H}}(P,Q) \leq \hat{d}_{\mathcal{H}}(P,Q) + C_1$$

Make P and Q as indistinguishable as possible e.g. minimize MMD, MK-MMD, domain discriminative loss, etc Decrease the upper bound on target risk !

# Today's Talk

- What's Transfer Learning
- Transfer Learning Techniques
  - Task transfer learning
  - Domain adaptation
  - Transfer bound on domain adaptation
- How to avoid negative transfer?
  - Case study on feature transferability in vision
  - Task transferability: empirical and theoretical methods
- Discussions and Q&A

# Where to start fine-tuning?

 Use pre-trained model as a fixed feature extractor

most efficient, but with limited performance

Fine-tune all the way

slow, easy to overfit when target labels are few

Fine-tune first k layers
 How to choose k?



# Which layers to transfer?

Yosinski et.al. (2014) How transferable are features in deep neural networks?

A case study using ImageNet classification tasks (trained on 7 CNN layers + output layer)

#### Dissimilar tasks

- Task A: Man-made object classification
- Task B: Natural object classification



# Which layers to transfer?

Yosinski et.al. (2014) How transferable are features in deep neural networks?

A case study using ImageNet classification tasks (trained on 7 CNN layers + output layer)

- Similar tasks: Random A/B split (500 classes in each task)
- Dissimilar tasks: Man-made (A) -> Natural (B)



transferability gap grows as the distance between tasks increases
features transferred from distant tasks are better than random features!

#### Fine-Tune Selected Layers

Guo et.al. (2019) SpotTune: Transfer Learning through Adaptive Fine-tuning

• for each training instance, adaptively decide which sets of layers to fine tune



Zamir et.al. (2018) Taskonomy: Disentangling Task Transfer Learning

investigated the transferability among 26 image-based indoor scene understanding tasks on low-data scenario

#### Main steps:

- 1. train task-specific networks (source models) on all data
- 2. For each S-T task pair, train a transfer network on a small validation dataset (20,000 images)



Zamir et.al. (2018) Taskonomy: Disentangling Task Transfer Learning

• Visual transferability results



#### On Validation Dataset (1/60 training data)

Zamir et.al. (2018) Taskonomy: Disentangling Task Transfer Learning

Raw losses from transfer functions have different scales



• Naive solution: linear rescale

performance increases at different speed with respective to loss !

Zamir et.al. (2018) Taskonomy: Disentangling Task Transfer Learning

 Analytic Hierarchy Process (AHP): an ordinal normalization approach (Saaty 1987)



Can we estimate transferability without relying on gradient descent?

sed

sfer

# Measure Task Transferability Analytically

Bao & Li et.al. (2019) An Information-Theoretic Metric for Task Transfera Learning

A simple task transfer learning model (with linear fine-tuning)



Transferability from Task S to Task T

 $\mathfrak{T}(S,T) \triangleq \frac{\text{Target Performance of } f_S}{\text{Optimal Target Performance}}$ 

$$\begin{cases} \mathfrak{T}(S,T) = 1 & \textcircled{0} \\ 0 \leq \mathfrak{T}(S,T) \leq 1 \\ \mathfrak{T}(S,T) = 0 & \textcircled{0} \end{cases}$$

How to measure feature performance?

# Feature performance via local information geometry

- a statistical view of binary classification

• Binary hypothesis testing of m observations of x:

$$H_0: x \sim P_{X|Y=0}, \quad H_1: x \sim P_{X|Y=1}$$

• Error exponent *E<sub>f</sub>*: the asymptotic rate at which the error probability of f(x) decays as m increases

$$\lim_{m \to \infty} -\frac{1}{m} \log(P_e) = E$$

**Theorem.** (Huang et al. 2015) When  $P_{X|Y=0}$ ,  $P_{X|Y=1}$ , and  $P_X$  are locally distributed, for some constant c > 0

$$E_f = c \mathcal{H}(f)$$
  
H-score of f(X



 $\mathcal{H}(f) = \operatorname{tr}(\operatorname{cov}(f(X))^{-1} \operatorname{cov}(\mathbb{E}_{P_{X|Y}}[f(X)|Y]))$ 

# An Information-Theoretic Metric for Transferability

 $\mathfrak{T}(S,T) \triangleq \frac{\text{Target Performance of } f_S}{\text{Optimal Target Performance}} = \frac{\mathscr{H}_T(f_S)}{\mathscr{H}_T(f_T^*)}$ 

H-score of source feature  $\mathcal{H}_T(f_S)$ 

- Easy to compute
- O(mk<sup>2</sup>) time complexity

Maximal H-score:  $\mathscr{H}_T(f_T^*)$ 

```
def Hscore(f,Y):<br/>Covf=np.cov(f)Python Code<br/>for H-ScorealphabetY=list(set(Y))<br/>g=np.zeros_like(f)<br/>for z in alphabetY:<br/>g[Y==y]=np.mean(f[Y==y,:], axis=0)<br/>Covg=np.cov(g)<br/>score=np.trace(np.dot(np.linalg.pinv(Covf,<br/>rcond=1e-15), Covg))<br/>return score
```

- Discrete X: Alternating Conditional Expectation (ACE) algorithm Makur et. al. (2015) An Efficient algorithm for information decomposition and extraction

# An Information-Theoretic Metric for Transferability

- Source task: ImageNet 1000 classification (ResNet50 features from 6 layers 4a-4f)
- Target task: Cifar 100-class classification on 20,000 images





# An Information-Theoretic Metric for Transferability















Query Image

2D Edges

3D (Occlusion) Edges

2D Keypoints

3D Keypoints

Image Reshading



Comparison with Task Affinity Score on 8 vision tasks.

- > 6 times faster
- top three most transferable source tasks are consistent with Task Affinity on most target tasks

easy-to-compute, efficient transferability metric with strong operational meaning!



#### **Rank Comparison**

# Other Analytical Transferability Metrics

• Transferability metrics for different transfer settings

Algorithm	<b>Different Tasks</b> $P(Y_S   X_S) \neq P(Y_T   X_T)$	<b>Different Instance</b> $X_S \neq X_T$	<b>Different Domain</b> $P(X_S) \neq P(X_T)$
NCE (Tran et al. 2019) *	$\checkmark$	×	×
H-Score (Bao et al. 2019)	$\checkmark$	$\checkmark$	×
LEEP (Nguyen et al. 2020)**	$\checkmark$	$\checkmark$	×
OTCE (Y. Tan et al. <i>under</i> <i>review</i> )	$\checkmark$	$\checkmark$	$\checkmark$

\* Anh T Tran, Cuong V Nguyen, and Tal Hassner. Transfer- ability and hardness of supervised classification tasks. ICCV, 2019. \*\* Cuong V Nguyen, Tal Hassner, Cedric Archambeau, and 952 Matthias Seeger. Leep: A new measure to evaluate trans- 953 ferability of learned representations.ICML, 2020.

# Today's Talk

- What's Transfer Learning
- Transfer Learning Techniques
  - Task transfer learning
  - Domain adaptation
  - Transfer bound on domain adaptation
- How to avoid negative transfer?
  - Case study on feature transferability
  - Task transferability: empirical and theoretical methods
- Discussions and Q&A

# **Open Theoretical Questions**

Can we find a transferability metric that ...

- accounts for domain difference
- depends on target sample-size
  - Rademacher complexity for computable transfer bound (Maurer 2009)
- depends on learning algorithm
  - Kolmogorov complexity-based task relatedness (Mahmud 2007)

# Beyond Transfer Learning

- Multi-source transfer learning: how to efficiently, adaptively combine features from multiple source tasks in transfer learning?
- Meta learning: given data/experience on previous tasks, learn a new task more quickly
  - transfer learning is one common approach in meta learning



challenge: efficient meta learning for heterogeneous tasks

### References & Resources

#### Book

• Yang, Q et al. (2019). Transfer Learning. Cambridge University Press

#### Survey papers

- Tan, C., Sun, F., Kong, T., Zhang, W., Yang, C., & Liu, C. (2018). A survey on deep transfer learning. Lecture Notes in Computer Science, 11141 LNCS, 270-279.
- Lisa Torrey and Jude Shavlik (2009). Transfer learning. Handbook of Research on Machine Learning Applications
- Pan, S.J., Yang, Q. (2010). A survey on transfer learning. IEEE Transactions on knowledge and data engineering 22(10), 1345-1359

#### Related web links:

- An Information-Theoretic Metric for Task Transfer Learning: <u>http://yangli-feasibility.com/home/</u> <u>ttl.html</u>
- Disentangling Task Transfer Learning: <u>http://taskonomy.stanford.edu/</u>

